

Probing the Stability of Many-Body Localization

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Controlling quantum matter: From ultracold atoms to solids, Vilnius, 01.08.2018



Magnetic Polarons in Fermi Hubbard Systems

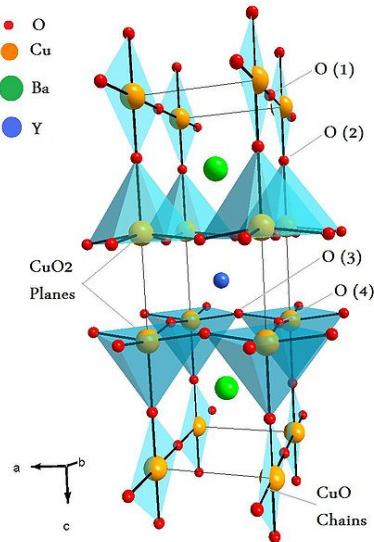
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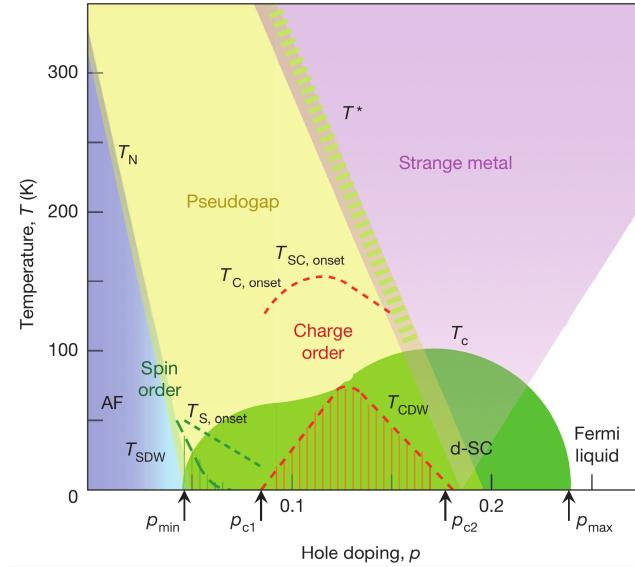


The physics of complex solid state materials



Wikipedia

Cuprate unit cell
(YBa₂Cu₃O₇)



Keimer, Nature 2015

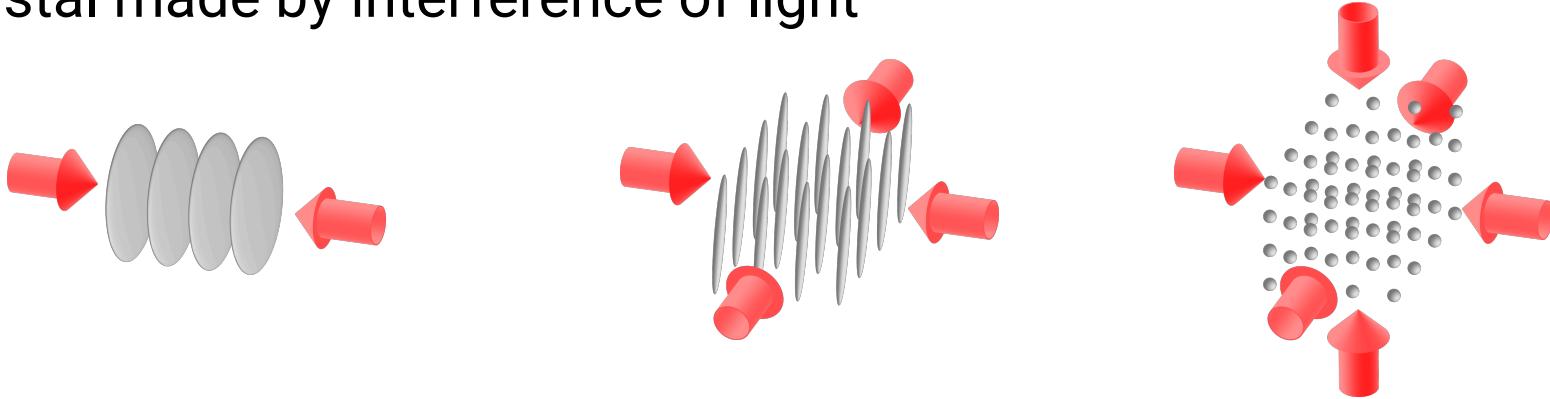
Prominent electronic toy model: **Hubbard model**

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$

Review: Lee, RMP 2006

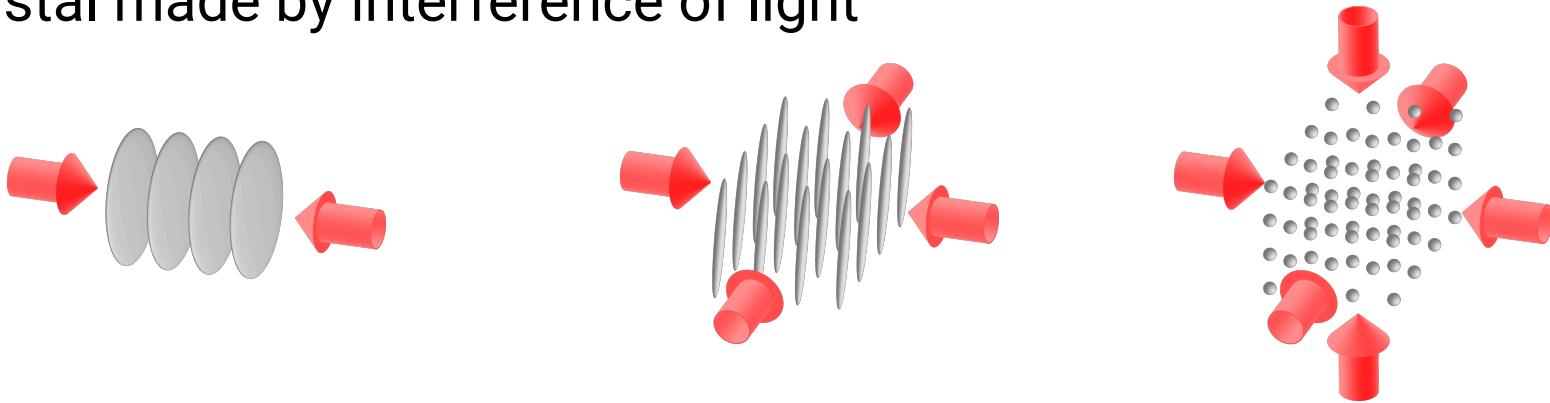
Hubbard models in optical lattices

A crystal made by interference of light



Hubbard models in optical lattices

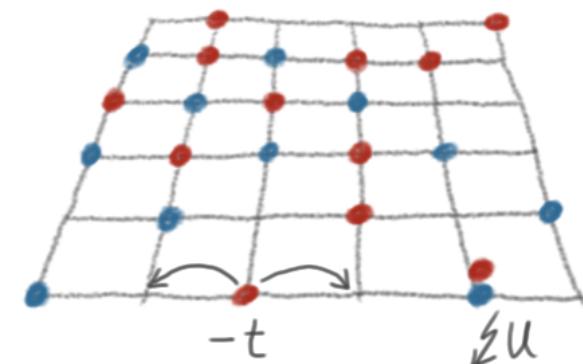
A crystal made by interference of light



Mobile quantum particles in the lattice - Hubbard models

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$

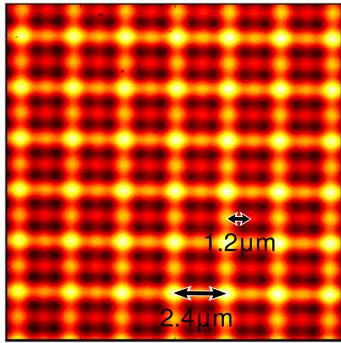
Emerging magnetic energy scale $J = \frac{4t^2}{U}$



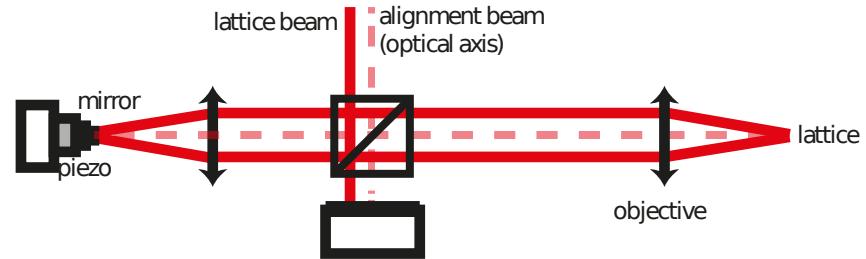
A specialized quantum gas microscope



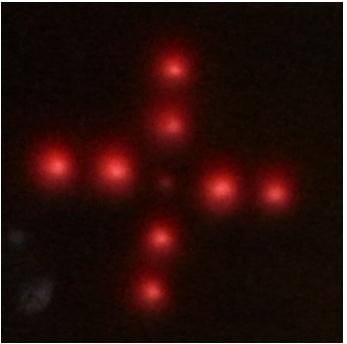
Fourier plane



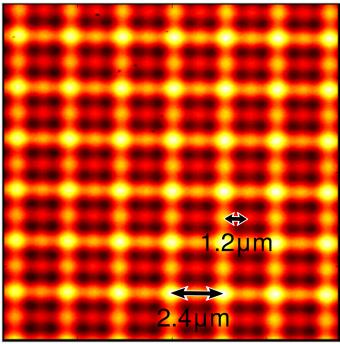
Atomic plane



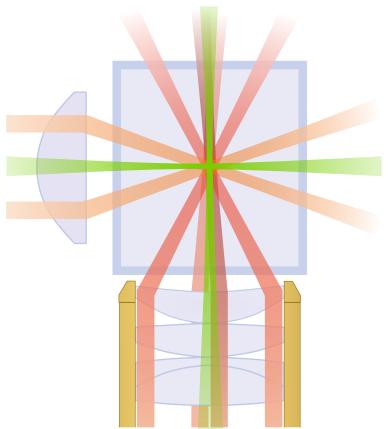
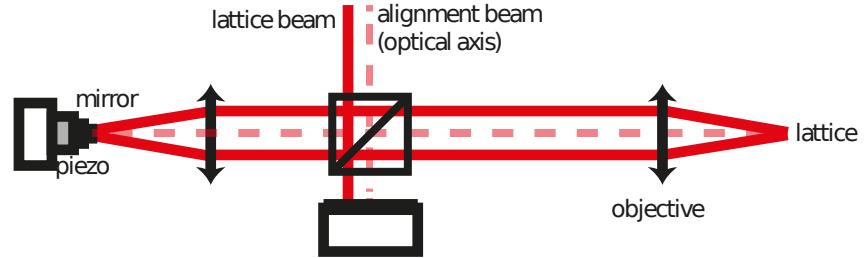
A specialized quantum gas microscope



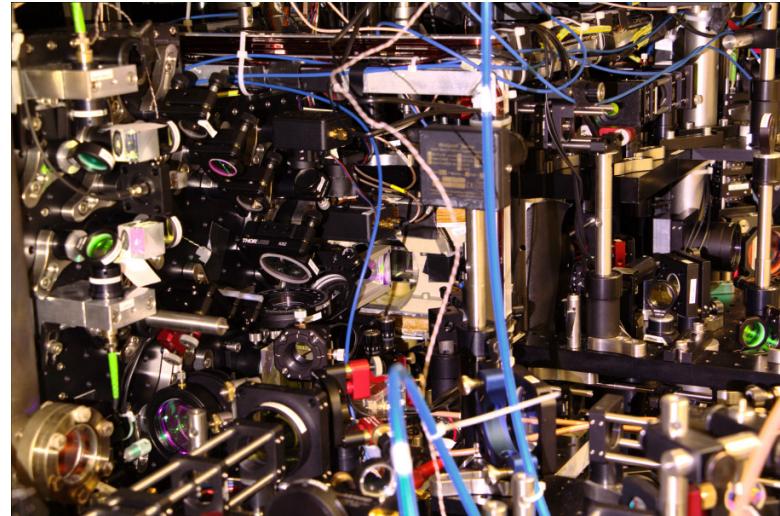
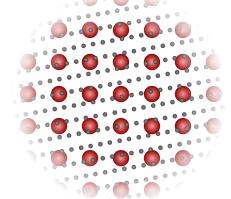
Fourier plane



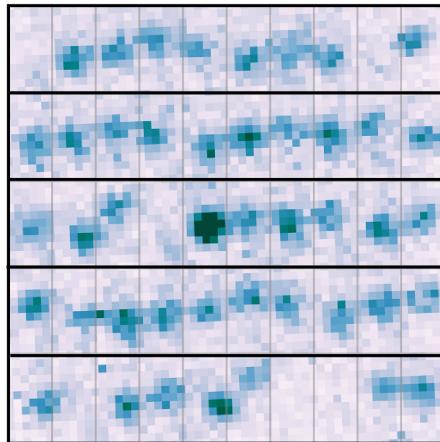
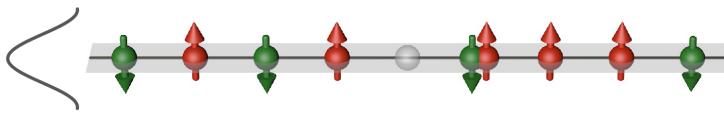
Atomic plane



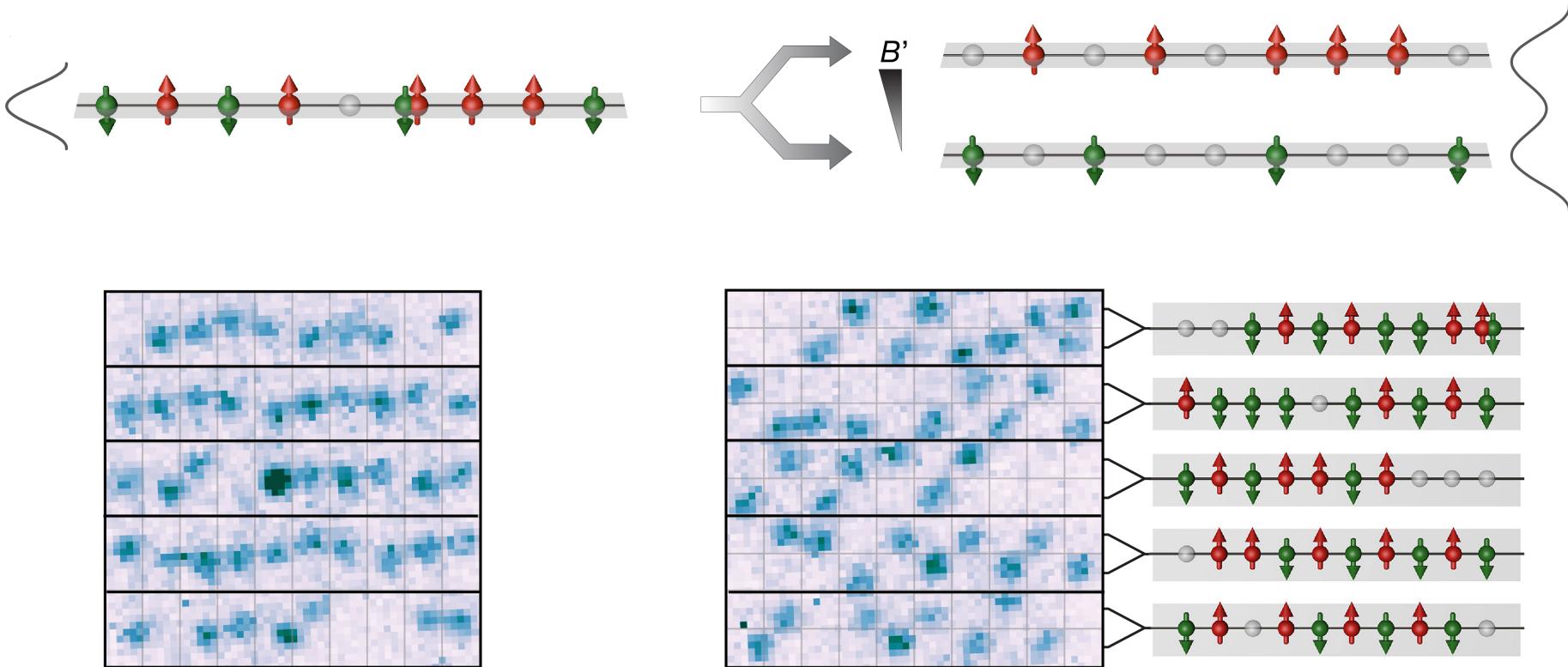
Independent
optical lattices
for imaging



Imaging spins and "charges"



Imaging spins and "charges"

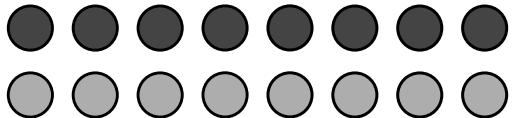


Full local information: Density and Spin
Access to spin-spin and spin-density correlations

Doping the 1d Hubbard model

Charge sector: Delocalization

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$



Spin sector: Antiferromagnetism

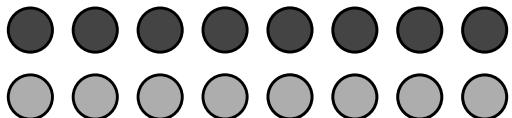
$$\hat{H}_{\text{Heis}} = J \sum_i \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_{i+1}$$



Doping the 1d Hubbard model

Charge sector: Delocalization

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$



Spin sector: Antiferromagnetism

$$\hat{H}_{\text{Heis}} = J \sum_i \hat{\mathbf{S}}_i \cdot \hat{\mathbf{S}}_{i+1}$$



What is the spin alignment around holes?

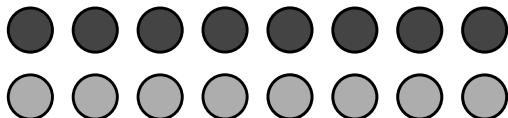
$$|\Psi\rangle = | \text{green} \text{ red} \text{ open circle} \text{ green} \text{ red} \rangle$$

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What is the spin alignment around holes?

$$|\Psi\rangle = | \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{green}{\triangledown} \textcolor{red}{\triangle} + \textcolor{green}{\triangledown} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} \textcolor{red}{\triangle} + \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} \textcolor{black}{\circ} \textcolor{red}{\triangle} + \dots \rangle$$

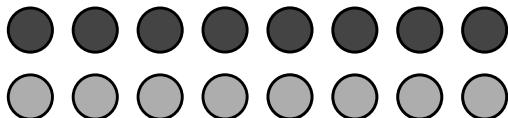
$$|\Psi\rangle = | \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} + \textcolor{green}{\triangledown} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} + \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{red}{\triangledown} \textcolor{black}{\circ} \textcolor{green}{\triangledown} + \dots \rangle$$

J J

Doping the 1d Hubbard model

Charge sector: Delocalization

$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$



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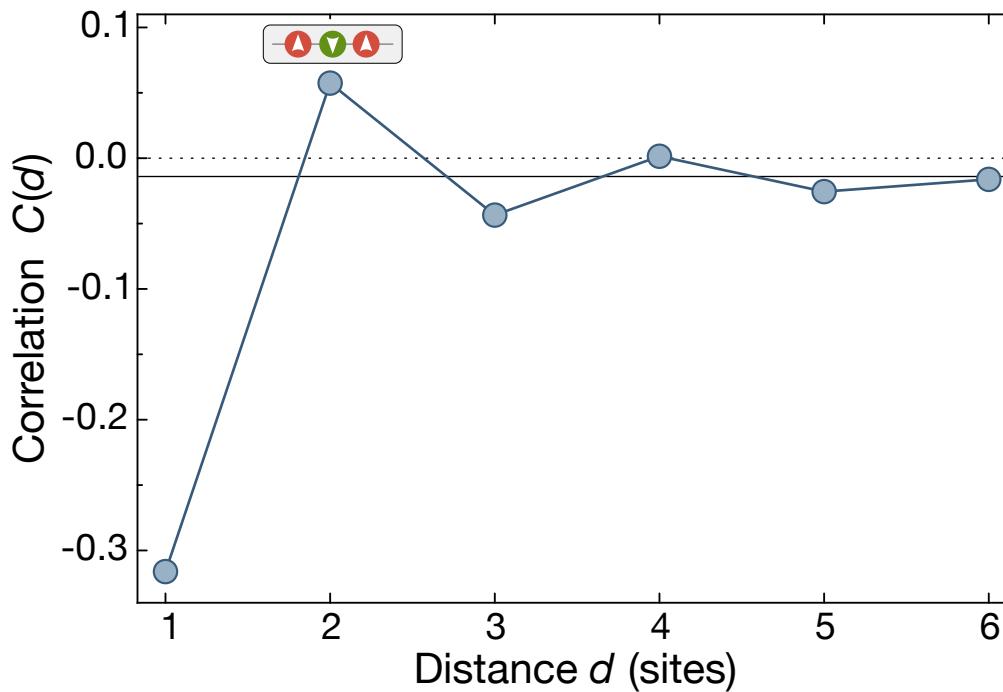
$$|\Psi\rangle = | \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{green}{\triangledown} \textcolor{red}{\triangle} + \textcolor{green}{\triangledown} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} \textcolor{red}{\triangle} + \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} \textcolor{black}{\circ} \textcolor{red}{\triangle} + \dots \rangle$$

$$|\Psi\rangle = | \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{green}{\triangledown} + \textcolor{green}{\triangledown} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} + \textcolor{green}{\triangledown} \textcolor{red}{\triangle} \textcolor{black}{\circ} \textcolor{black}{\circ} \textcolor{red}{\triangle} \textcolor{green}{\triangledown} + \dots \rangle$$

J J

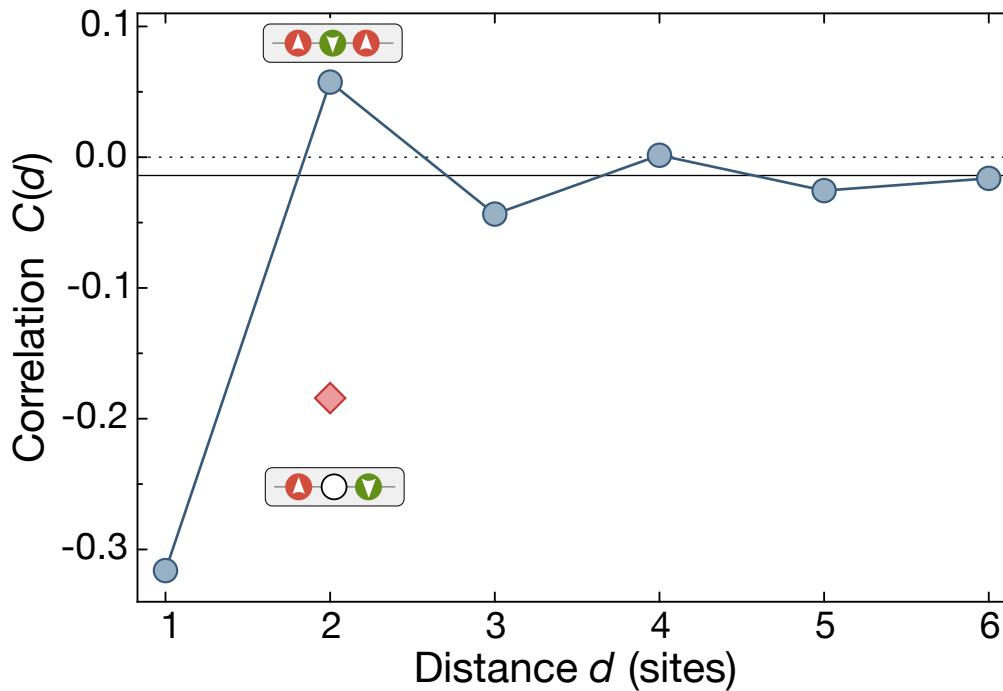
Spin alignment across holes

$$C_{SH, N_h}(d) = 4 \langle \hat{S}_i^z \hat{S}_{i+d}^z \rangle \bigcirc_i \{\bullet\}_{N_h} \bigcirc_{i+d}$$



Spin alignment across holes

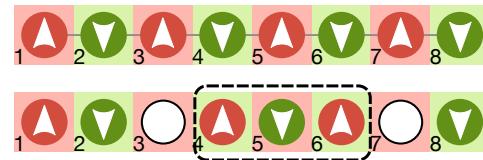
$$C_{SH, N_h}(d) = 4 \langle \hat{S}_i^z \hat{S}_{i+d}^z \rangle \bigcirc_i \{\bullet\}_{N_h} \bigcirc_{i+d}$$



Hidden correlations

AFM parity flips suppress the standard 2-point correlator

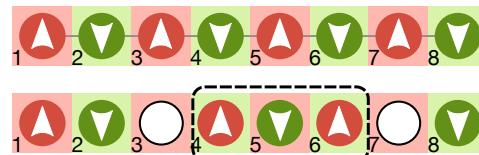
$$C(d) = 4 \left(\langle \hat{S}_i^z \hat{S}_{i+d}^z \rangle_{\bullet_i \bullet_{i+d}} - \langle \hat{S}_i^z \rangle_{\bullet_i} \langle \hat{S}_{i+d}^z \rangle_{\bullet_{i+d}} \right)$$



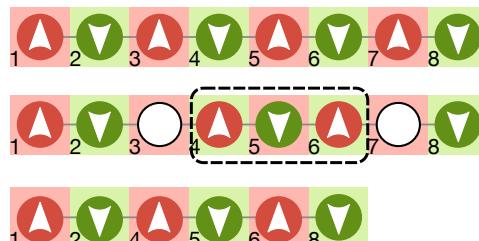
Hidden correlations

AFM parity flips suppress the standard 2-point correlator

$$C(d) = 4 \left(\langle \hat{S}_i^z \hat{S}_{i+d}^z \rangle_{\bullet_i \bullet_{i+d}} - \langle \hat{S}_i^z \rangle_{\bullet_i} \langle \hat{S}_{i+d}^z \rangle_{\bullet_{i+d}} \right)$$



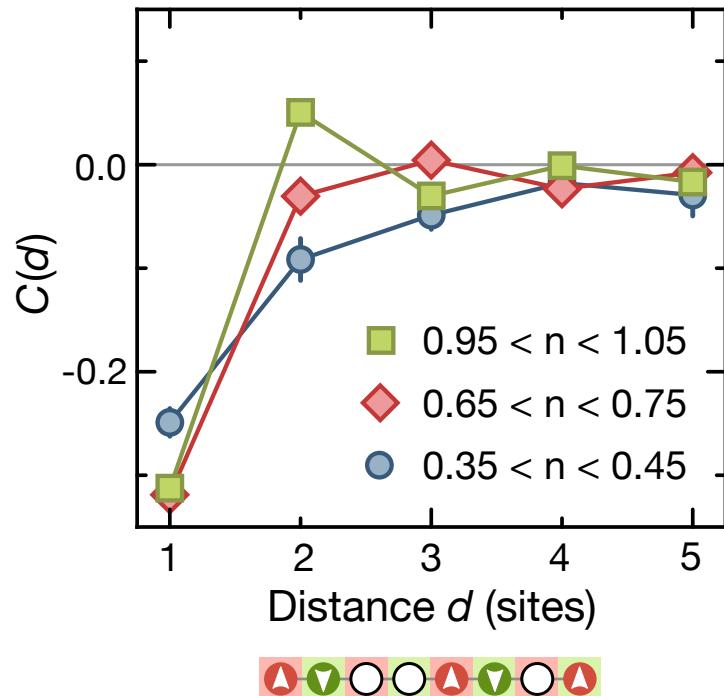
Reveal **hidden** spin correlations in "squeezed space"



→ discard sites with holes

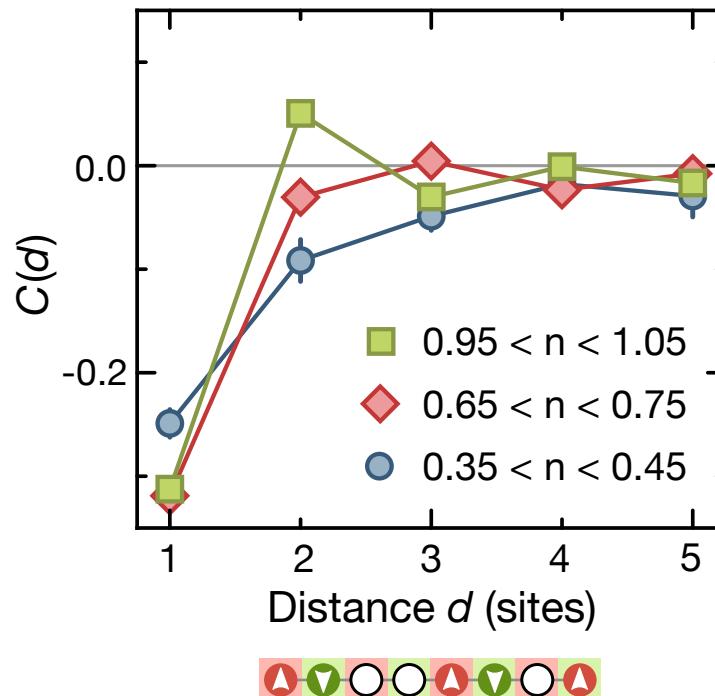
Correlations in squeezed space

Standard 2-point correlator

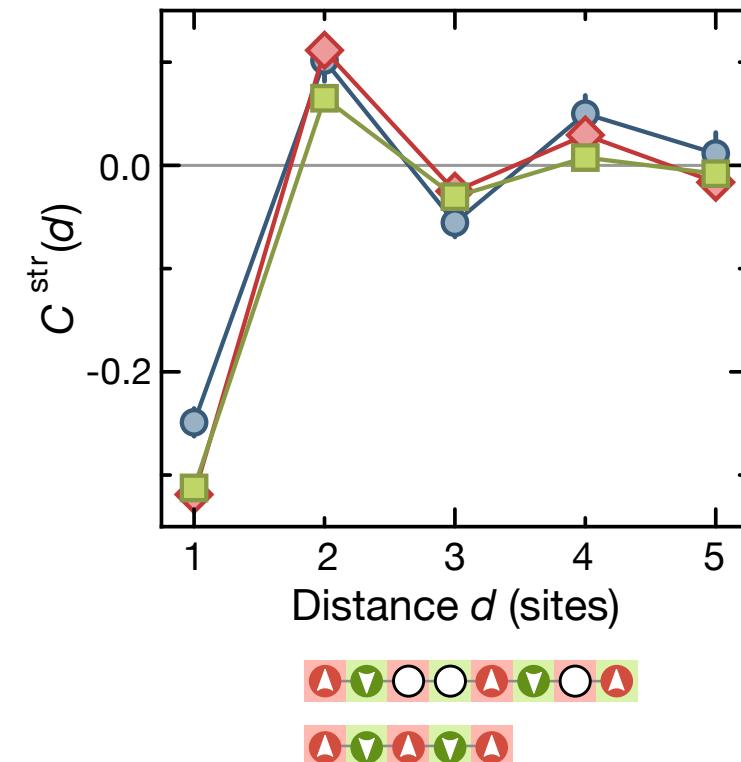


Correlations in squeezed space

Standard 2-point correlator



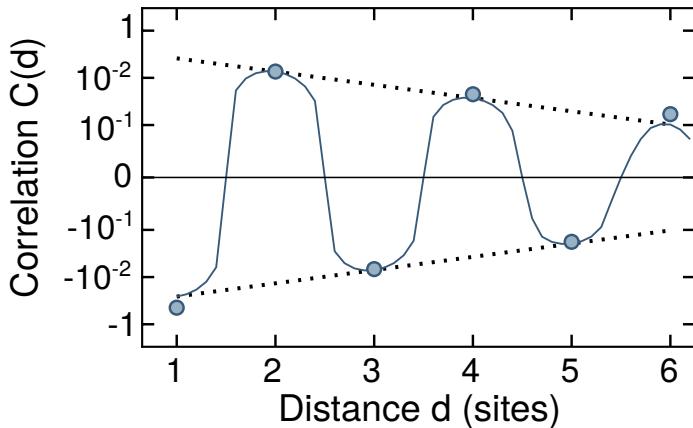
Squeezed space 2-point correlator



→ Spin-charge separation

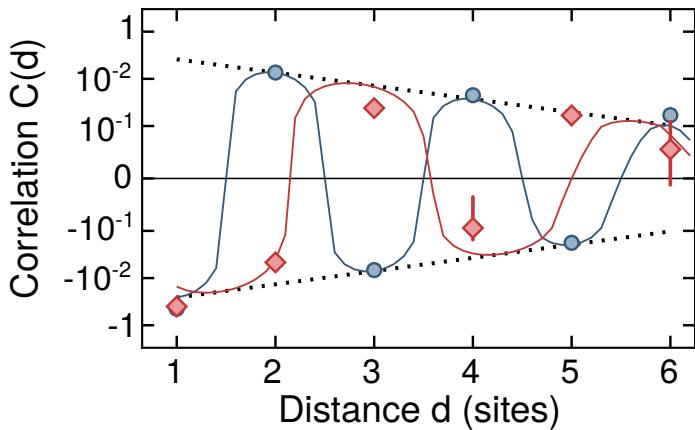
Incommensurate magnetism - charge

Holes / Doublons dilute (stretch) the spin correlations



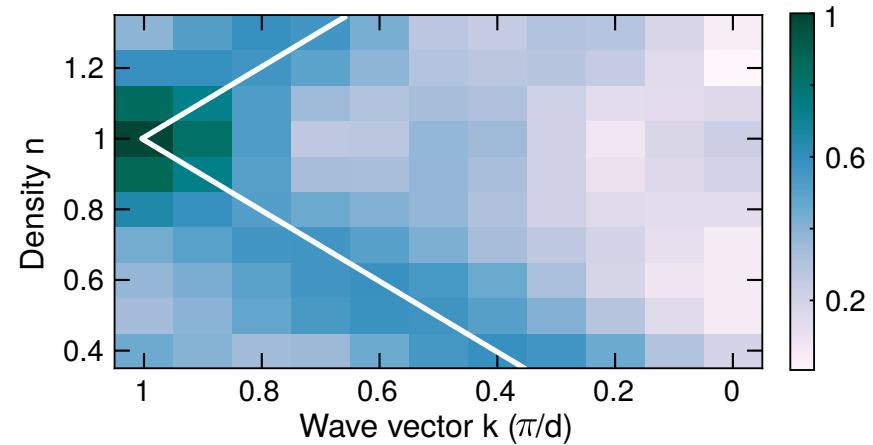
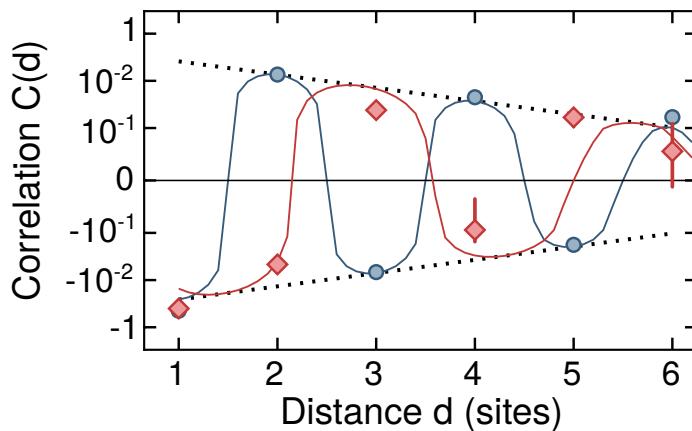
Incommensurate magnetism - charge

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Incommensurate magnetism - charge

Holes / Doublons dilute (stretch) the spin correlations



Linear density dependence of the wave vector
 (as expected by Luttinger theory)

$$\langle \hat{S}_i^z \hat{S}_{i+d}^z \rangle \propto \cos(\pi(1 - n_h)d)$$

Thank you!

The Lithiums



Guillaume



Joannis



Timon



Jayadev



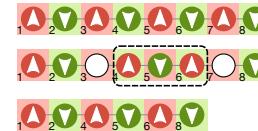
Mim



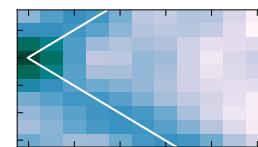
Immanuel

+ Eugene and Fabian @ Harvard

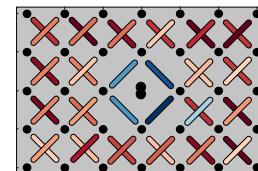
Summary



Hidden magnetism
spin-charge separation



Incommensurate
magnetism



Magnetic polarons